

1) If  $f(x, y) = 2x + 3x^2y$  find the following:

a)  $\int_0^3 f(x, y) \, dx$

b)  $\int_0^4 f(x, y) \, dy$

a) 
$$\boxed{9+27y}$$

b) 
$$\boxed{8x+24x^2}$$

2) Calculate the following iterated integrals:

a)  $\int_1^3 \int_0^1 (1+4xy) \, dx \, dy$

b)  $\int_0^2 \int_0^{\pi/2} x \sin y \, dy \, dx$

c)  $\int_0^1 \int_1^2 \frac{xe^x}{y} \, dy \, dx$

d)  $\int_0^{\ln 2} \int_0^{\ln 5} e^{2x-y} \, dx \, dy$

a) 
$$\boxed{10}$$

b) 
$$\boxed{2}$$

c) 
$$\boxed{\ln 2}$$

d) 
$$\boxed{6}$$

3) Calculate the following double integrals:

a)  $\iint_R (6x^2y^3 - 5y^4) \, dA, \quad R = \{(x, y) \mid 0 \leq x \leq 3, 0 \leq y \leq 1\}$

b)  $\iint_R \frac{xy^2}{x^2+1} \, dA, \quad R = \{(x, y) \mid 0 \leq x \leq 1, -3 \leq y \leq 3\}$

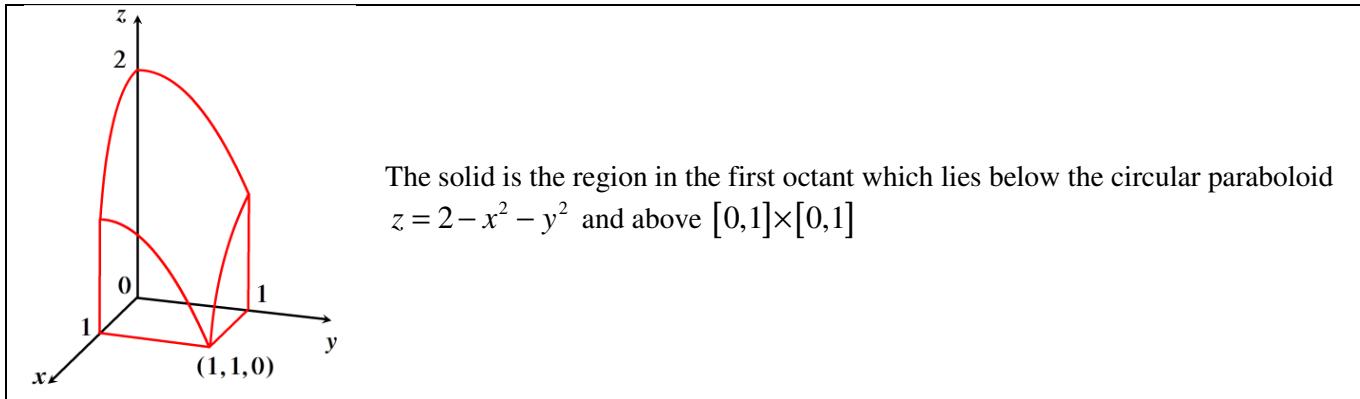
c)  $\iint_R \frac{x}{1+xy} \, dA, \quad R = [0,1] \times [0,1]$

a) 
$$\boxed{\frac{21}{2}}$$

b) 
$$\boxed{9\ln 2}$$

c) 
$$\boxed{2\ln 2 - 1}$$

- 4) Sketch the solid whose volume is given by the iterated integral  $\int_0^1 \int_0^1 (2 - x^2 - y^2) dy dx$ .



- 5) Find the volume of the solid that lies under the hyperbolic paraboloid  $z = 4 + x^2 - y^2$  and above the square  $R = [-1,1] \times [0,2]$ .

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- 6) Find the volume of the solid bounded by the elliptic paraboloid  $z = 1 + (x-1)^2 + 4y^2$ , the planes  $x=3$  and  $y=2$ , and the coordinate planes.

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